

# **Extracting Position and Velocity Information in a Software GPS Receiver**

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# GPS Software-Defined Receiver

## General Principle:

**GPS signal is sampled as close to antenna as practical and remainder of signal processing takes place in a microprocessor**

- More versatile than traditional architectures
- Allows parallel development at all stages
- Signal propagation is more readily analyzed

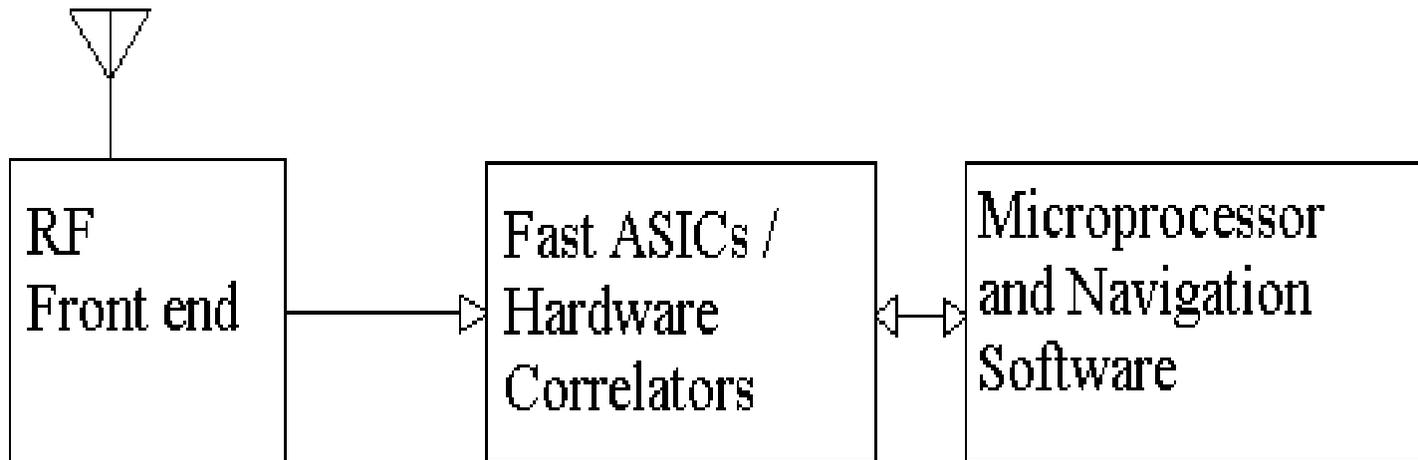


# Research Motivation

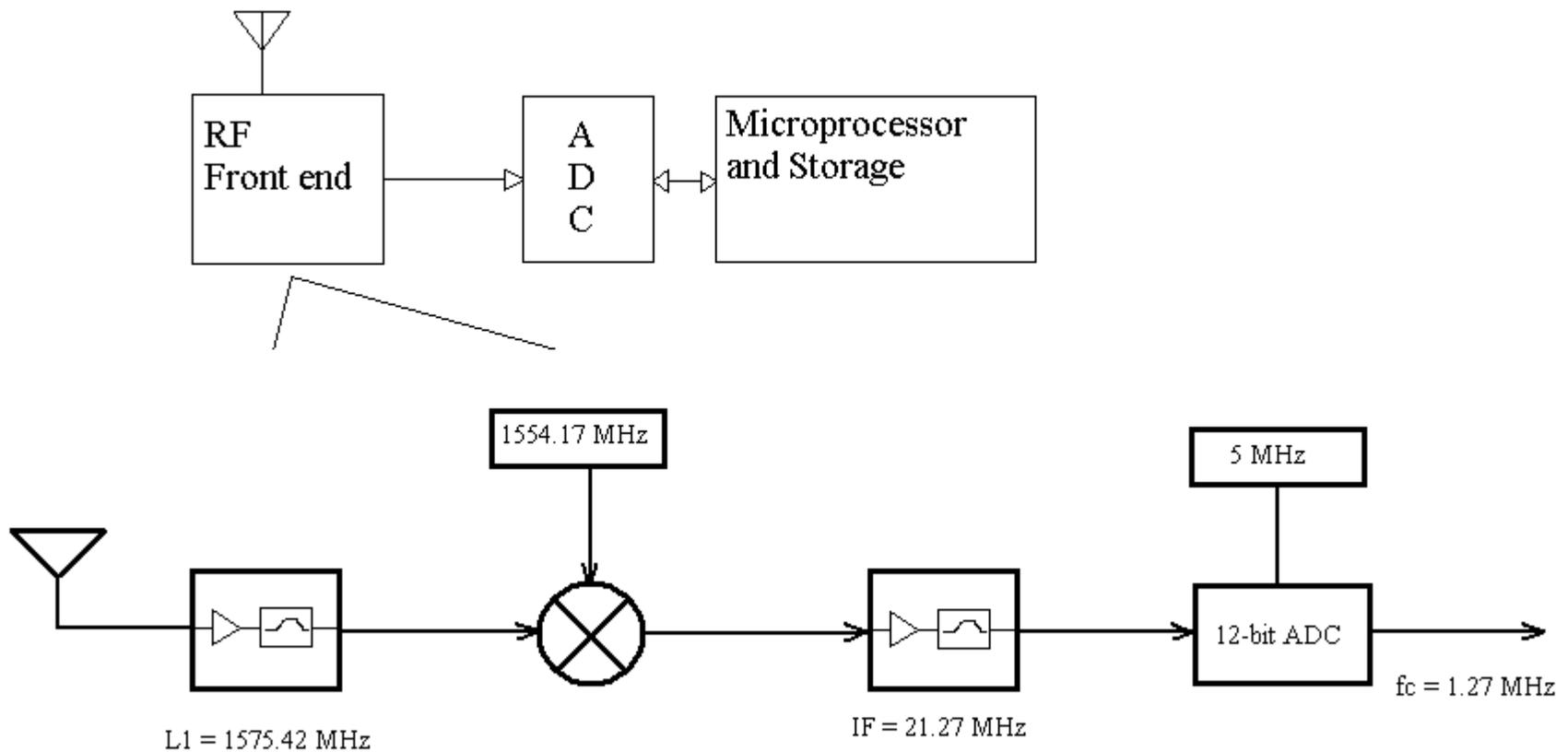
- Previous studies of signal tracking revealed code-carrier divergence
- This problem would not raise concern in a communications software radio
- The uncertainty imposes an obstacle in high-accuracy carrier applications



# Tradition Receiver Architecture (High-Level)

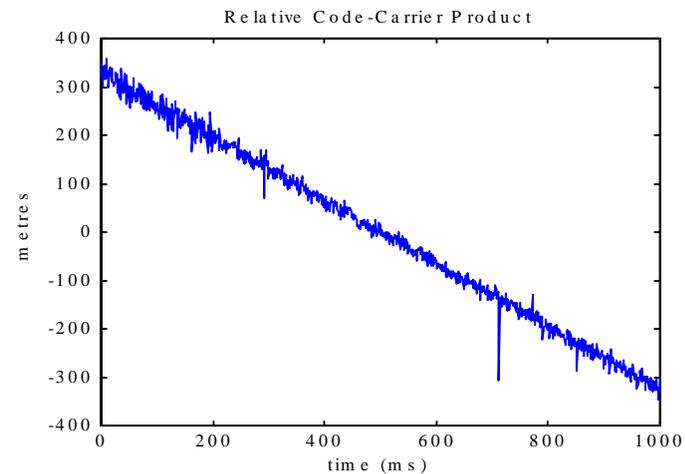
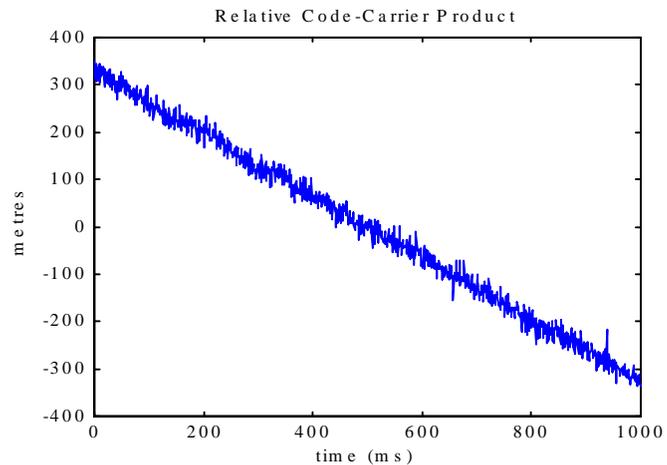
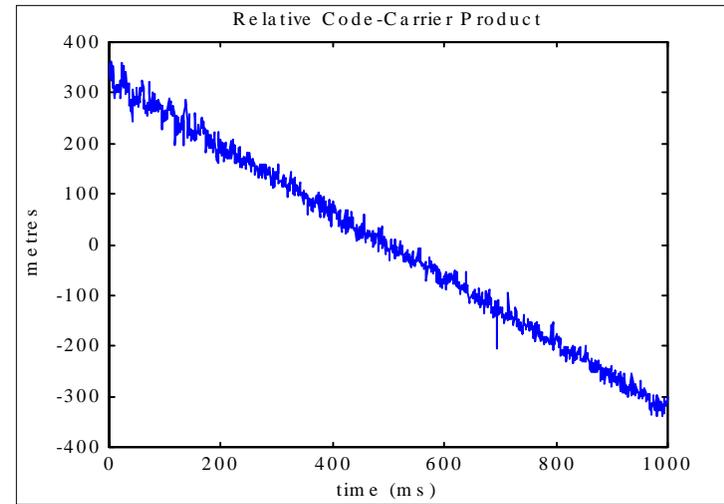
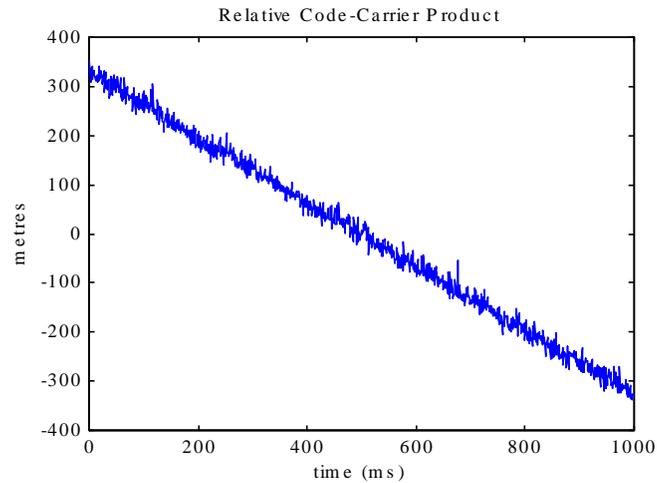


# Software Receiver Architecture (High-Level)

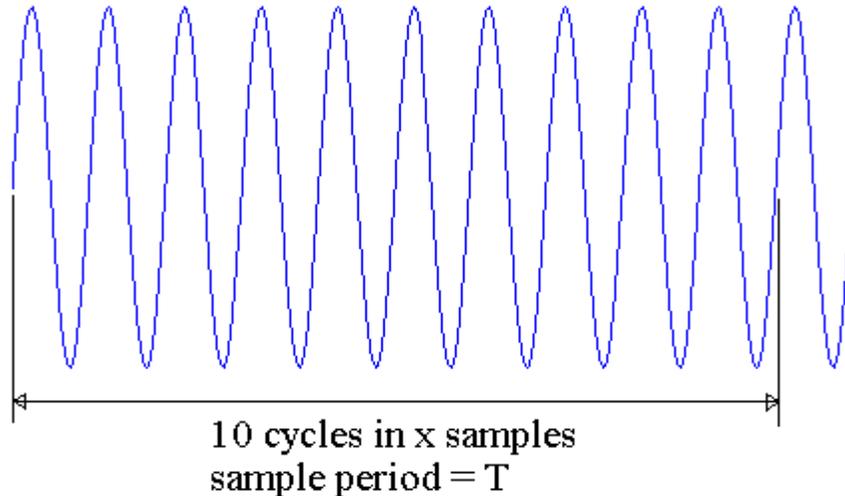


# Initial Results

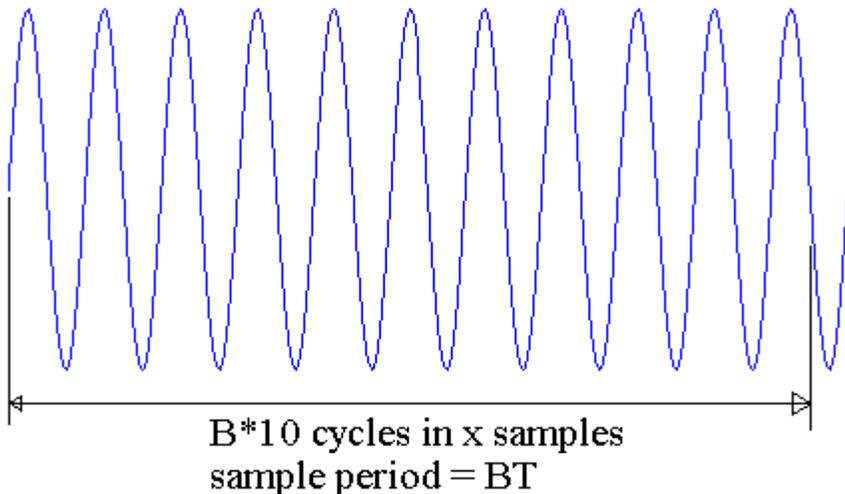
## Code - carrier ranges on 4 satellites:



# Sample Doppler



**Apparent effect of a sample period error factor  $BT$  is a Doppler frequency error factor  $Bf$**



**Therefore, a sampling oscillator error of  $1/B$  leads to a SAMPLE DOPPLER  $B$**



# Signal Downconversion and Sampling

$\gamma$  True Doppler Scale Factor

$\epsilon$  Local Oscillator Error Scale Factor

$f_C = \gamma f_{L1} - \epsilon f_{LO}$  Downconversion, No Sampling

$f_C = \beta (\gamma f_{L1} - \epsilon f_{LO})$  Conventional Sampling

$f_C = \beta (\gamma f_{L1} - \epsilon f_{LO}) - \beta M f_S$  Bandpass Sampling

$M = \text{floor} (f_{IF} / f_S)$  Number of “Folds” in Scheme



# Velocity Measurements

Carrier velocity measurements are based on calculated Doppler:

$$f_{nom} = f_{L1} - f_{LO} - Mf_S$$

$$f_{Dop} = f_C - f_{nom}$$

$$= (\beta\gamma - 1) f_{L1} - (1 - \beta\epsilon) f_{LO} - (\beta - 1) Mf_S$$

$$V_{CAR} = f_{Dop} \lambda_{L1} = c(\beta\gamma - 1) - (1 - \beta\epsilon) f_{LO} \lambda_{L1} - (\beta - 1) Mf_S \lambda_{L1}$$



# Velocity Measurements

Code velocity measurements can be based on chip rate:

$$R_{CODE} = \gamma\beta R_{nom}$$

$$R_{Dop} = R_{CODE} - R_{nom} = (\gamma\beta - 1)R_{nom}$$

$$V_{CODE} = R_{Dop} \lambda_{chip} = c(\gamma\beta - 1)$$

**The velocities may be subtracted to yield a residual:**

$$V_{C-C} = (1 - \beta\varepsilon) f_{LO} \lambda_{L1} + (\beta - 1) M f_S \lambda_{L1}$$

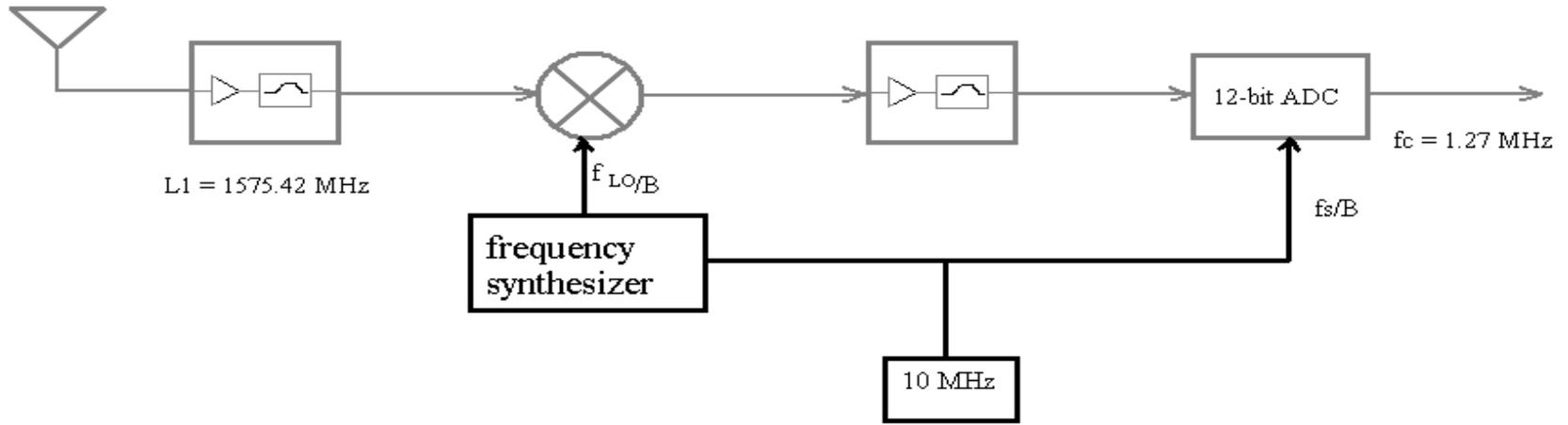


# Residual Code-Carrier Velocity

- Remaining velocity term is not dependent on  $\gamma$ , and is thus the same for all SVs
- Contains terms of LO error and sample Doppler, which cannot be decoupled with one measurement
- This effect is not observed in a traditional receiver



# New Front End



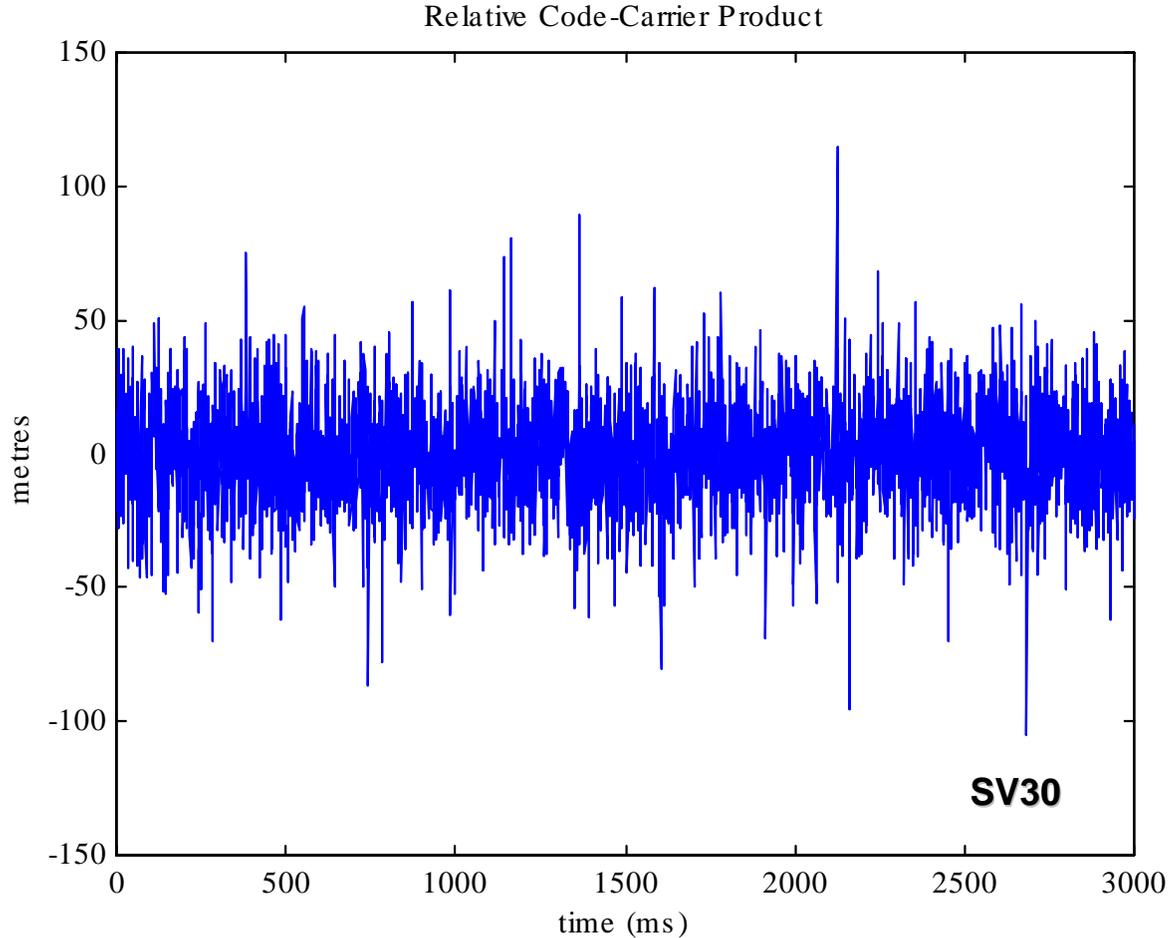
- LO and sample clock driven by same oscillator

$$V_{C-C} = (1 - \beta \epsilon) f_{LO} \lambda_{L1} + (\beta - 1) M f_S \lambda_{L1}$$

$$V_{C-C} = \left(1 - \beta \frac{1}{\beta}\right) f_{LO} \lambda_{L1} + (\beta - 1) M f_S \lambda_{L1}$$

$$V_{C-C} = (\beta - 1) M f_S \lambda_{L1}$$

# Code-Carrier (New Front End)



# Conclusions

- **Divergence in initial results was due to a local oscillator error that affected the carrier, but not the code**
- **Remaining divergence term due to sample Doppler may be present, but is likely to be very small**
- **Further improvements on front end will allow higher SNR and better determination of data trends**



# Continuing Work

- **Obtain cleaner data sets from hardware**
- **Collect longer records for navigation data extraction and decoding**
- **Seek and explore new tracking methods to boost performance expectations**

